CBSE Board

Class IX Mathematics

Sample Paper 5

Time: 3 hrs Total Marks: 80

General Instructions:

- 1. All questions are compulsory.
- 2. The question paper consists of 30 questions divided into four sections A, B, C, and D. Section A comprises of 6 questions of 1 mark each, Section B comprises of 6 questions of 2 marks each, Section C comprises of 10 questions of 3 marks each and Section D comprises of 8 questions of 4 marks each.
- **3.** Use of calculator is **not** permitted.

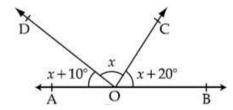
Section A (Questions 1 to 6 carry 1 mark each)

1. What is the decimal form of $\frac{11}{1000}$?

OR

Is zero a rational number? Justify.

- 2. x + y = 2 and x y = 4. Find the values of x and y.
- 3. In the given figure, find the value of x?



4. If for one of the solutions of the equation ax + by + c = 0, x is negative and y is positive, then a portion of the above line will lie in which Quadrant?

OR

The cost of 5 pencils is equal to the cost of 2 ballpoints. Write a linear equation

d 102.

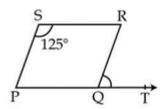
Determine the Class size?







6. PQRS is a parallelogram in which \angle PSR = 125°. Find \angle RQT.



Section B (Questions 7 to 12 carry 2 marks each)

- If $a = 2 + \sqrt{3}$, find the value of $a + \frac{1}{2}$.
- The perpendicular distance of a point from the x-axis is 2 units and the perpendicular 8. distance from the y-axis is 5 units. Write the coordinates of such a point if it lies in one of the following quadrants:
 - (i) I Quadrant (ii) II Quadrant
- (iii) III Quadrant
- (iv) IV Quadrant
- 9. The total surface area of a cube is 294 cm². Find its volume.

A matchbox measures $4 \text{ cm} \times 2.5 \text{ cm} \times 1.5 \text{ cm}$. What is the volume of a packet containing 12 such matchboxes?

- 10. Check which of the following are solutions of the equation 7x 5y = -3.
 - i. (-1, -2)
 - ii. (-4, -5)

OR

Explain linear equations in two variables.

- 11. Find the area of an isosceles triangle with base 10 cm and perimeter 36 cm.
- 12. Simplify: $(-2x + 5y 3z)^2$.

Section C (Questions 13 to 22 carry 3 marks each)

13. Express 0.001 as a fraction in the simplest form.

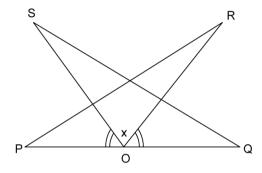
OR

Simplify
$$\frac{\sqrt{a^2 - b^2} + a}{\sqrt{a^2 + b^2} + b} \div \frac{\sqrt{a^2 + b^2} - b}{a - \sqrt{a^2 - b^2}}$$

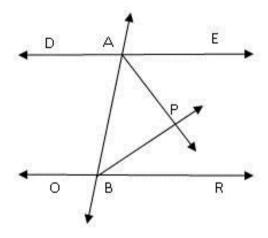
14. Find the value of $x^3 - 8y^3 - 36xy - 216$ when x = 2y + 6.

Find the remainder when $x^3 + 3x^2 + 3x + 1$ is divided by $x + \pi$.

15. In the figure, PQ is a line segment and 0 is the mid-point of PQ. R and S are on the same side of PQ such that \angle PQS = \angle QPR and \angle POS = \angle QOR. Prove that



- (i) $\Delta PQR \cong \Delta QOS$
- (ii) PR = QS
- 16. If the polynomials $az^3 + 4z^2 + 3z 4$ and $z^3 4z + a$ leave the same remainder when divided by z 3, then find the value of a.
- 17. In the given figure, DE \parallel OR and AP and BP are bisectors of \angle EAB and \angle RBA, respectively. Find \angle APB.





18. The following frequency distribution table gives the weights of 38 students of a class.

Weight in kg	Number of students
30 - 35	10
35 - 40	5
40 – 45	15
45 – 50	5
50 – 55	1
55 – 60	2
Total	38

Find the probability that the weight of students is

- i. more than or equal to 45 Kg
- ii. less than 30 kg
- iii. more than or equal to 30 Kg but less than 60 Kg
- 19. Find the area of the triangle formed by A (0, 4), O(0, 0) and B(3, 0).
- 20. If $x = 1 + \sqrt{2}$, find the value of $\left(x \frac{1}{x}\right)^3$.

OR

Find the value of $x^3 + y^3 - 12xy + 64$ when x + y = -4.

21. A wooden article was made by scooping out a hemisphere from each end of a solid cylinder. If the height of the cylinder is 10 cm and its base is 7 cm, find the total surface area of the article.

OR

How much cardboard is required to make 35 penholders in the shape of cylinders, each of radius 3 cm and height 10.5 cm?



22. The length of 40 leaves of a plant are measured correct to one millimeter, and the data obtained is represented in the following table:

Length (in mm)	Number of leaves
118 - 126	3
127 - 135	5
136 - 144	9
145 – 153	12
154 - 162	5
163 – 171	4
172 – 180	2

- i. Draw a histogram to represent the given data.
- ii. Is there any other suitable graphical representation for the same data?
- iii. Is it correct to conclude that maximum leaves are 153 mm long? Why?

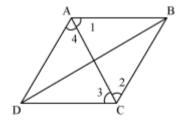
Section D (Questions 23 to 30 carry 4 marks each)

23. Simplify:
$$\frac{3\sqrt{2} - 2\sqrt{3}}{3\sqrt{2} + 2\sqrt{3}} + \frac{\sqrt{12}}{\sqrt{3} - \sqrt{2}}$$

OR

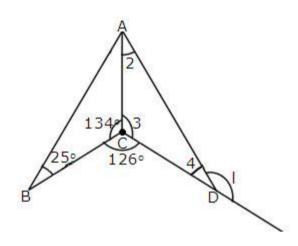
Express
$$\frac{3}{\sqrt{3}-\sqrt{2}+\sqrt{5}}$$
 with rational denominator.

24. ABCD is a rhombus. Show that the diagonal AC bisects $\angle A$ as well as $\angle C$ and diagonal BD bisects $\angle B$ as well as $\angle D$.



- 25. If the polynomial $x^4 + mx^3 25x^2 16x + n$ is exactly divisible by $x^2 4$, then what are the values of m and n?
- 26. In the given figure, AC is the bisector of $\triangle BAD$. Find the measures of $\angle 1, \angle 2, \angle 3$ and $\angle 4$.





27. A cube and cuboid have the same volume. The dimensions of the cuboid are in the ratio 1:2:4. If the difference between the cost of polishing the cube and cuboid at the rate of Rs. 5 per m^2 is Rs. 80, find their volumes.

OR

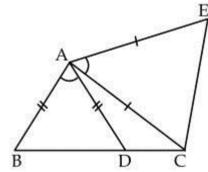
30 circular plates, each of radius 14 cm and thickness 3 cm are placed one above the other to form a cylindrical solid. Find the total surface area and volume of the cylinder formed.

28. If O is point lying inside ΔXYZ , then show that (OX + OY + OZ) cannot be less than the semi-perimeter of ΔXYZ .

OR

Show that the bisectors of the base angles of a triangle can never enclose a right angle.

29. In the given figure, AC = AE, AB = AD and \angle BAD = \angle EAC. Prove that BC = DE.



30. If $m = \frac{1}{2 - \sqrt{3}}$ and $n = \frac{1}{2 + \sqrt{3}}$, then what is the value of $7m^2 + 11mn - 7n^2$?



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Class IX Mathematics

Sample Paper 5 - Solution

Time: 3 hrs Total Marks: 80

Section A

1.
$$\frac{11}{1000} = 0.011$$

OR

Yes, because 0 can be written as $\frac{0}{1}$ which is of the form $\frac{p}{q}$, where p and q are integers and $q \neq 0$.

- 2. x + y = 2(i) and x - y = 4(ii) Adding (i) and (ii), we get x = 3Putting x = 3 in the equation (i), we get y = -1 $\therefore x = 3$ and y = -1
- 3. Since AOB is a Straight Line,

only positive numbers.

$$\therefore \angle AOD + \angle COD + \angle COB = 180^{\circ}$$

$$\therefore x + 10^{\circ} + x + x + 20^{\circ} = 180^{\circ}$$

$$\therefore 3x = 150^{\circ}$$

$$\therefore x = 50^{\circ}$$

4. If for one of the solutions of the equation ax + by + c = 0, x is negative and y is positive, then a portion of the above line definitely lies in the II Quadrant.As in the II Quadrant the x-axis contains only negative numbers and y-axis contains

OR

Let the cost of a pencil to be Rs. x and that of a ballpoint to be Rs. y. Hence, the linear equation is 5x = 2y5x - 2y = 0.





- 5. Here the class marks are uniformly spaced,
 - Therefore,
 - Class size is the difference between any two consecutive class marks.
 - :. Class Size = 52 47 = 5
- 6. $\angle PSR = \angle RQP = 125^{\circ}$ (since PQRS is a parallelogram, then the opposite angles will be equal)
 - \therefore \angle PQT = 180°.....(PQT is a straight line)
 - $\therefore \angle PQR + \angle RQT = 180^{\circ}$
 - $\therefore 125^{\circ} + \angle RQT = 180^{\circ}$
 - $\therefore \angle RQT = 55^{\circ}$

Section B

7.
$$a = 2 + \sqrt{3}$$

$$\Rightarrow \frac{1}{a} = \frac{1}{2 + \sqrt{3}}$$

$$= \frac{1}{2 + \sqrt{3}} \times \frac{2 - \sqrt{3}}{2 - \sqrt{3}}$$

$$= \frac{2 - \sqrt{3}}{2^2 - (\sqrt{3})^2}$$

$$= 2 - \sqrt{3}$$
So, $a + \frac{1}{a} = (2 + \sqrt{3}) + (2 - \sqrt{3}) = 4$

- 8. (i) I quadrant: (5, 2)
 - (ii) II quadrant: (-5, 2)
 - (iii) III quadrant: (-5, -2)
 - (iv) IV quadrant: (5, -2)
- 9. Let 'l' be the length of the cube.

Now, T.S.A. of the cube = 294 cm^2 ...(given)

- $\therefore 6l^2 = 294$
- \therefore Side, l = 7 cm

Volume of cube = $1 \times 1 \times 1 = 7 \times 7 \times 7 = 343$ cm³

OR

According to the question,

Volume of one matchbox = $4 \text{ cm} \times 2.5 \text{ cm} \times 1.5 \text{ cm} = 15 \text{ cm}^3$

Volume of 12 such matchboxes = $15 \times 12 = 180 \text{ cm}^3$





10. Given equation is 7x - 5y = -3

i.
$$(-1, -2)$$

Putting x = -1 and y = -2 in the L.H.S. of the given equation, we get

$$7x - 5y = 7(-1) - 5(-2) = -7 + 10 = 3 \neq R.H.S.$$

Hence, (-1, -2) is not a solution of this equation.

ii.
$$(-4, -5)$$

Putting x = -4 and y = -5 in the L.H.S. of the given equation, we get

$$7x - 5y = 7(-4) - 5(-5) = -28 + 25 = -3 = R.H.S.$$

Hence, (-4, -5) is a solution of this equation.

OR

An equation of the form ax + by + c = 0, where a, b, c are real numbers such that $a \ne 0$ and $b \ne 0$, is called a linear equation in two variables x and y.

11. Perimeter = 36 cm = 10 cm + 2(Length of an equal side)

Here,
$$s = \frac{36}{2} = 18$$
, and the sides are 10, 13 and 13.

By Heron's formula,

Area =
$$\sqrt{18 \times 8 \times 5 \times 5}$$
 = 60 sq. cm

12.
$$(-2x + 5y - 3z)^2$$

$$= (-2x)^2 + (5y)^2 + (-3z)^2 + 2(-2x)(5y) + 2(5y)(-3z) + 2(-2x)(-3z)$$

$$=4x^2+25y^2+9z^2-20xy-30yz+12zx$$

Section C

13. Let
$$x = 0.\overline{001}$$

Then,
$$x = 0.001001001...$$
 (i)

Therefore,
$$1000x = 1.001001001...$$
 (ii)

Subtracting (i) from (ii), we get,

$$999x = 1 \Rightarrow x = \frac{1}{999}$$

Hence,
$$0.\overline{001} = \frac{1}{999}$$





$$\begin{split} \frac{\sqrt{a^2 - b^2} + a}{\sqrt{a^2 + b^2} + b} & \div \frac{\sqrt{a^2 + b^2} - b}{a - \sqrt{a^2 - b^2}} = \frac{\sqrt{a^2 - b^2} + a}{\sqrt{a^2 + b^2} + b} \times \frac{a - \sqrt{a^2 - b^2}}{\sqrt{a^2 + b^2} - b} \\ & = \frac{a^2 - \left(\sqrt{a^2 - b^2}\right)^2}{\left(\sqrt{a^2 + b^2}\right)^2 - b^2} \\ & = \frac{a^2 - \left(a^2 - b^2\right)}{\left(a^2 + b^2\right) - b^2} \\ & = \frac{a^2 - a^2 + b^2}{a^2 + b^2 - b^2} \\ & = \frac{b^2}{a^2} \end{split}$$

14. Given:
$$x = 2y + 6$$
 or $x - 2y - 6 = 0$

We know that if a + b + c = 0, then $a^3 + b^3 + c^3 = 3xyz$

Therefore, we have:

$$(x)^3 + (-2y)^3 + (-6)^3 = 3x(-2y)(-6)$$

Or,
$$x^3 - 8y^3 - 36xy - 216 = 0$$

OR

Let
$$p(x) = x^3 + 3x^2 + 3x + 1$$
 and $g(x) = x + \pi$

Now,
$$g(x) = 0$$

$$x + \pi = 0$$

$$x = -\pi$$

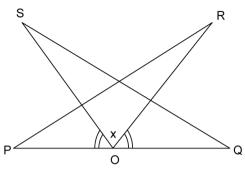
By the remainder theorem, when p(x) is divided by $x + \pi$ then the remainder is $p(-\pi)$.

$$p(-\pi) = (-\pi)^3 + 3(-\pi)^2 + 3(-\pi) + 1 = -\pi^3 + 3\pi^2 - 3\pi + 1$$

Hence, remainder is $-\pi^3 + 3\pi^2 - 3\pi + 1$.



15.



In ΔPOR and ΔQOS

$$\angle QPR = \angle PQS$$
 (given)

OP = OQ (O is the mid-point of PQ)

$$\angle POS = \angle QOR$$
 (given)

$$\angle POS + x^0 = \angle QOR + x^0$$

$$\angle POR = \angle QOS$$

By ASA congruence rule,

$$\Delta PQR \cong \Delta QOS$$

$$\Rightarrow$$
 PR = QS (By CPCT)

16. Let
$$p(z) = az^3 + 4z^2 + 3z - 4$$
 and $q(z) = z^3 - 4z + a$

When p(z) is divided by z - 3, the remainder is given by

$$p(3) = a \times 3^3 + 4 \times 3^2 + 3 \times 3 - 4$$

$$= 27a + 36 + 9 - 4$$

$$= 27a + 41$$
(i)

When q(z) is divided by z - 3, the remainder is given by

$$q(3) = 3^3 - 4 \times 3 + a$$

$$= 27 - 12 + a$$

$$= 15 + a$$
(ii)

Given that p(3) = q(3).

So, from (i) and (ii), we have

$$27a + 41 = 15 + a$$

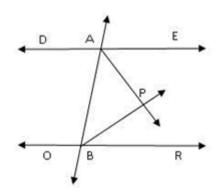
$$27a - a = -41 + 15$$

$$26a = -26$$

$$a = -1$$



17. Since interior angles on the same side of transversal are supplementary.



Therefore, $\angle EAB + \angle RBA = 180^{\circ}$

$$\frac{1}{2} \angle EAB + \frac{1}{2} \angle RBA = \frac{1}{2} \times 180^{\circ}$$
(i)

As AP and BP are bisectors of \angle EAB and \angle RBA respectively,

$$\angle PAB = \frac{1}{2} \angle EAB \text{ and } \angle PBA = \frac{1}{2} \angle RBA \qquad \dots \text{(ii)}$$

From (i) and (ii), we get

$$\angle PAB + \angle PBA = 90^{\circ}$$

In \triangle APB, we have

$$\angle$$
 PAB + \angle PBA + \angle APB = 180°

$$\Rightarrow$$
 90° + \angle APB = 180°

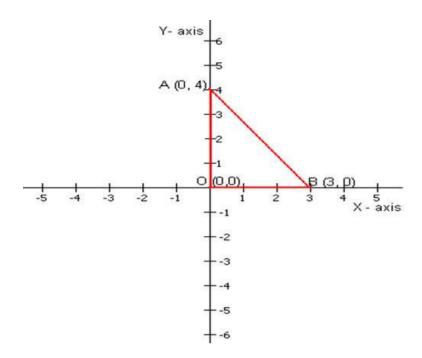
$$\Rightarrow$$
 \angle APB = 180° - 90° = 90°

- 18. Total number of students = 38
 - i. Number of students weighing more than or equal to 45 kg = 5 + 1 + 2 = 8
 - ∴ P(a student weighing more than or equal to 45 kg) = $\frac{8}{38} = \frac{4}{19}$
 - ii. Number of students weighing less than 30 kg = 0
 - ∴ P(a student weighing less than 30 kg) = $\frac{0}{38}$ = 0
 - iii. Number of students weighing more than or equal to 30 kg but less than 60 kg

$$=10+5+15+5+1+2$$

- = 38
- \therefore Required probability = $\frac{38}{38} = 1$

19. The given points A(0, 4), O(0, 0), B(3, 0) can be plotted as follows:



Clearly, AOB is a right-angled triangle.

OA = 4 units, OB = 3 units.

Area of $\triangle AOB = \frac{1}{2} \times Base \times Height = \frac{1}{2} \times 3 \times 4 = 6 \text{ square units}$

20. Given,
$$x = 1 + \sqrt{2}$$

And,
$$\frac{1}{x} = \frac{1}{1 + \sqrt{2}}$$

$$= \frac{1}{1 + \sqrt{2}} \times \frac{1 - \sqrt{2}}{1 - \sqrt{2}}$$

$$= \frac{1 - \sqrt{2}}{1^2 - (\sqrt{2})^2}$$

$$= -1 + \sqrt{2}$$
Now, $\left(x - \frac{1}{x}\right) = \sqrt{2} + 1 - (\sqrt{2} - 1) = 2$

$$\therefore \left(x - \frac{1}{x}\right)^3 = 2^3 = 8$$

OR

$$x^{3} + y^{3} - 12xy + 64$$

= $x^{3} + y^{3} + 4^{3} - 3xy \times 4$
= $x^{3} + y^{3} + z^{3} - 3xyz$ where $z = 4$
= $(x + y + z)(x^{2} + y^{2} + z^{2} - xy - yz - zx)$
= $(x + y + 4)(x^{2} + y^{2} + 16 - xy - 4y - 4x)$ $\therefore z = 4$



$$= (-4 + 4)(x^{2} + y^{2} + 16 - xy - 4y - 4x)$$

$$= 0$$
Hence, $x^{3} + y^{3} - 12xy + 64 = 0$.

21. Base radius,
$$r = \frac{7}{2} = 3.5 \text{ cm}$$

Height of the cylinder, h = 10 cm

Curved surface area of cylinder = $2\pi rh$

$$= 2 \times \pi \times 3.5 \times 10$$
$$= 70\pi \text{ cm}^2$$

Curved surface area of two hemisphere = $2 \times 2\pi r^2$

$$= 4 \times \pi \times 3.5^{2}$$
$$= 49\pi \text{ cm}^{2}$$

 \therefore Total surface area = $70\pi + 49\pi = 374$ cm²

OR

Cardboard required to make 1 penholder = Curved surface area + area of the base

$$= 2\pi rh + \pi r^{2}$$

$$= \pi r (2h + r)$$

$$= \frac{22}{7} \times 3 \times \left(2 \times \frac{21}{2} + 3\right)$$

$$= \frac{22}{7} \times 3 \times 24$$

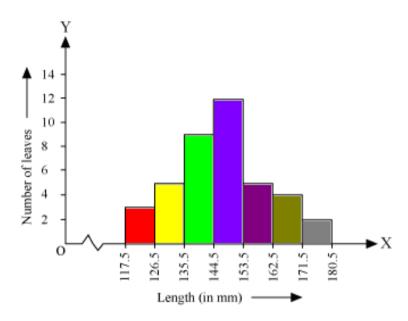
Cardboard required to make 35 penholders. = $\frac{22}{7} \times 3 \times 24 \times 35 = 7920 \text{ cm}^2$

22. Lengths of the leaves are represented in discontinuous class intervals. Hence we have to add 0.5 mm to each upper class limit and also have to subtract 0.5 mm from the lower class limits so as to make our class intervals continuous.

Length (in mm)	Number of leaves
117.5 – 126.5	3
126.5 – 135.5	5
135.5 – 144.5	9
144.5 – 153.5	12
153.5 – 162.5	5
162.5 – 171.5	4
171.5 - 180.5	2

i. Now taking the length of leaves on the x-axis and number of leaves on the y-axis we can draw the histogram of this information as below:





Here 1 unit on the y-axis represents 2 leaves.

- ii. Other suitable graphical representation of this data could be a frequency polygon.
- iii. No, as maximum numbers of leaves (i.e. 12) have their length in between of 144.5 mm and 153.5 mm. It is not necessary that all have a length of 153 mm.



23.

We have,

$$\frac{3\sqrt{2} - 2\sqrt{3}}{3\sqrt{2} + 2\sqrt{3}} + \frac{\sqrt{12}}{\sqrt{3} - \sqrt{2}}$$

$$= \frac{3\sqrt{2} - 2\sqrt{3}}{3\sqrt{2} + 2\sqrt{3}} \times \frac{3\sqrt{2} - 2\sqrt{3}}{3\sqrt{2} - 2\sqrt{3}} + \frac{\sqrt{12}}{\sqrt{3} - \sqrt{2}} \times \frac{\sqrt{3} + \sqrt{2}}{\sqrt{3} + \sqrt{2}}$$

$$= \frac{\left(3\sqrt{2} - 2\sqrt{3}\right)^2}{\left(3\sqrt{2} + 2\sqrt{3}\right)\left(3\sqrt{2} - 2\sqrt{3}\right)} + \frac{\sqrt{12}\left(\sqrt{3} + \sqrt{2}\right)}{\left(\sqrt{3} - \sqrt{2}\right)\left(\sqrt{3} + \sqrt{2}\right)}$$

$$= \frac{\left(3\sqrt{2}\right)^2 + \left(2\sqrt{3}\right)^2 - 2\times 3\sqrt{2}\times 2\sqrt{3}}{\left(3\sqrt{2}\right)^2 - \left(2\sqrt{3}\right)^2} + \frac{2\sqrt{3}\left(\sqrt{3} + \sqrt{2}\right)}{\left(\sqrt{3}\right)^2 - \left(\sqrt{2}\right)^2}$$

$$= \frac{18 + 12 - 12\sqrt{6}}{18 - 12} + \frac{6 + 2\sqrt{6}}{3 - 2}$$

$$= \frac{30 - 12\sqrt{6}}{6} + 6 + 2\sqrt{6}$$

$$= \frac{6\left(5 - 2\sqrt{6}\right)}{6} + 6 + 2\sqrt{6}$$

$$= 5 - 2\sqrt{6} + 6 + 2\sqrt{6}$$

$$= 11$$

$$\therefore \frac{3\sqrt{2} - 2\sqrt{3}}{3\sqrt{2} + 2\sqrt{3}} + \frac{\sqrt{12}}{\sqrt{3} - \sqrt{6}} = 11$$

OR

$$\frac{3}{\sqrt{3} - \sqrt{2} + \sqrt{5}} = \frac{3}{\sqrt{3} - \sqrt{2} + \sqrt{5}} \times \frac{\sqrt{3} - \sqrt{2} - \sqrt{5}}{\sqrt{3} - \sqrt{2} - \sqrt{5}}$$

$$= \frac{3(\sqrt{3} - \sqrt{2} - \sqrt{5})}{(\sqrt{3} - \sqrt{2})^2 - (\sqrt{5})^2}$$

$$= \frac{3(\sqrt{3} - \sqrt{2} - \sqrt{5})}{(3 + 2 - 2\sqrt{6}) - 5}$$

$$= \frac{3(\sqrt{3} - \sqrt{2} - \sqrt{5})}{-2\sqrt{6}}$$

$$= \frac{3(\sqrt{3} - \sqrt{2} - \sqrt{5})}{-2\sqrt{6}} \times \frac{\sqrt{6}}{\sqrt{6}}$$

$$= \frac{3(\sqrt{3} - \sqrt{2} - \sqrt{5})}{-2\sqrt{6}} \times \frac{\sqrt{6}}{\sqrt{6}}$$

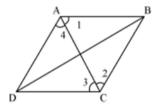
$$= \frac{3(\sqrt{18} - \sqrt{12} - \sqrt{30})}{-12}$$

$$= \frac{3(3\sqrt{2} - 2\sqrt{3} - \sqrt{30})}{-12}$$

$$= \frac{3\sqrt{2} - 2\sqrt{3} - \sqrt{30}}{-4}$$

$$= \frac{2\sqrt{3} + 3\sqrt{2} - \sqrt{30}}{4}$$

24. Let us join AC.



In AABC

BC = AB (sides of a rhombus)

 \therefore $\angle 1 = \angle 2$ (angles opposite to equal sides of a triangle are equal)

But $\angle 1 = \angle 3$ (alternate interior angles)

$$\Rightarrow \angle 2 = \angle 3$$

So, AC bisects $\angle C$.

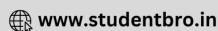
Also, $\angle 2 = \angle 4$ (alternate interior angles)

$$\Rightarrow \angle 1 = \angle 4$$

So, AC bisects ∠A

Similarly, we can prove that BD bisects $\angle B$ and $\angle D$ as well.





25. Let
$$p(x) = x^4 + mx^3 - 25x^2 - 16x + n$$
 and $g(x) = x^2 - 4 = (x + 2)(x - 2)$

Since p(x) is exactly divisible by g(x), p(x) is divisible by both (x + 2) and (x - 2).

Using factor therom, we have

$$p(-2) = 0$$

$$\Rightarrow$$
 $(-2)^4 + m(-2)^3 - 25(-2)^2 - 16(-2) + n = 0$

$$\Rightarrow$$
 16 - 8m - 100 + 32 + n = 0

$$\Rightarrow$$
 n - 8m - 52 = 0

Also,
$$p(2) = 0$$

$$\Rightarrow$$
 (2)⁴ + m(2)³ - 25(2)² - 16(2) + n = 0

$$\Rightarrow$$
 16 +8m - 100 -32 + n = 0

$$\Rightarrow$$
 n + 8m - 116 = 0

From equation (1) and (2), we get

$$n - 8m - 52 = n + 8m - 116$$

(Each is 0)

$$\Rightarrow$$
 - 8m - 52 = 8m - 116

$$\Rightarrow$$
 116 – 52 = 16m

$$\Rightarrow$$
 m = $\frac{64}{16}$ = 4

Substituting the value of m in equation (1),

$$n - 8(4) - 52 = 0$$

$$\Rightarrow$$
 n - 32 - 52 = 0

$$\Rightarrow$$
 n - 84 = 0

$$\Rightarrow$$
 n = 84

Thus, the values of m and n are 4 and 84 respectively.

26. Applying angle sum property in \triangle ABC, we have

$$\angle ABC + \angle BCA + \angle BAC = 180^{\circ}$$

$$\Rightarrow$$
 25° + 134° + \angle BAC = 180°

$$\Rightarrow$$
 \angle BAC = 180° – 1590 = 210

Now, AC is the bisector of $\angle BAD$.

$$\therefore \angle BAC = \angle CAD$$

$$(\because \angle BAC = 210)$$

We know that the measure of one complete angle is 3600.

$$\therefore \angle BCD + \angle BCA + \angle ACD = 360^{\circ}$$

$$\Rightarrow$$
 126° + 134° + \angle 3 = 360°

$$\Rightarrow$$
 $\angle 3 = 360^{\circ} - 260^{\circ} = 100^{\circ}$





By exterior angle property of triangles, we have

$$\angle 1 = \angle 2 + \angle 3$$

$$\Rightarrow$$
 $\angle 1 = 21^{\circ} + 100^{\circ} = 121^{\circ}$

By applying angle sum property in \triangle ACD, we have:

$$\angle ACD + \angle CDA + \angle CAD = 180^{\circ}$$

$$\Rightarrow$$
 100° + \angle 4 + 21° = 180°

$$\Rightarrow \angle 4 = 180^{\circ} - 121^{\circ} = 59^{\circ}$$

27. Let the dimensions of the cuboid are x, 2x and 4x.

Hence, volume of cuboid = $x \times 2x \times 4x = 8x^3$

Volume of cube = Volume of cuboid

- \therefore Volume of cube = $8x^3$ = side³
- \therefore Side of cube = 2x

Total Surface Area of cuboid = $2(lb + bh + hl) = 2(2x^2 + 8x^2 + 4x^2) = 28x^2$ Cost of polishing the cuboid = Rs. $5 \times 28x^2 = 140x^2$

Total Surface Area of cube = $6(\text{side})^2 = 6(2x)^2 = 24x^2$.

Cost of polishing the cube = Rs. $5 \times 24x^2 = 120x^2$

The difference between cost of polishing the cube and the cuboid is Rs. 80.

Hence,
$$140x^2 - 120x^2 = 80$$

$$\Rightarrow 20x^2 = 80$$

$$\Rightarrow$$
 $x^2 = 4$

$$\Rightarrow$$
 x = 2

Volume of cuboid = Volume of cube = $8 \times (2)^3$ m³ = 64 m³.

OR

The cylinder formed as base radius, r = 14 cm and height = $h = 3 \times 30 = 90$ cm

The total surface area = $2\pi rh + 2\pi r^2 = 2\pi r(h + r)$

$$= 2 \times \frac{22}{7} \times 14 + (90 + 14)$$

$$= 9152 \text{ cm}^2$$

Volume of the cylinder formed = $\pi r^2 h$

$$= \frac{22}{7} \times 14 \times 14 \times 90$$

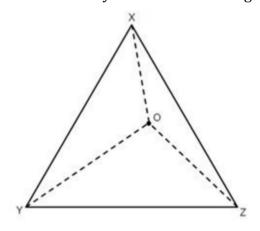
$$= 55440 \text{ cm}^3$$







28. The sum of any two sides of a triangle is always greater than the third side.



In
$$\Delta$$
OXY, OX + OY > XY(1)

In
$$\triangle OYZ$$
, $OY + OZ > YZ$ (2)

In
$$\Delta$$
OXZ, OX + OZ > XZ(3)

Adding equations (1), (2) and (3),

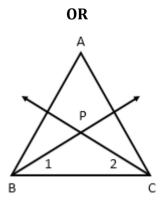
$$(OX + OY) + (OY + OZ) + (OX + OZ) > XY + YZ + ZX$$

$$2(OX + OY + OZ) > XY + YZ + ZX$$

$$OX + OY + OZ > \frac{1}{2} (XY + YZ + ZX)$$

$$OX + OY + OZ > Semi-perimeter of \Delta XYZ$$
.

Hence, (OX + OY + OZ) cannot be less than the semi-perimeter of ΔXYZ .



In ΔABC , BP and CP are bisectors of angles B and C respectively.

Hence,
$$\angle A + \angle B + \angle C = 180^{\circ}$$

$$\angle A + 2 \angle 1 + 2 \angle 2 = 180^{\circ}$$

$$2 \angle 1 + 2 \angle 2 = 180^{\circ} - \angle A$$

$$\angle 1 + \angle 2 = 90^{\circ} - \angle A/2....(1)$$





Ιη ΔΡΒC,

$$\angle P + \angle 1 + \angle 2 = 180^{\circ}$$

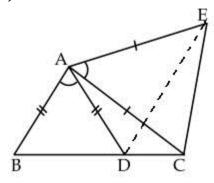
$$\angle P + [90^{\circ} - \angle A/2] = 180^{\circ}$$
 from (i)

$$\angle P = 180^{\circ} - [90^{\circ} - \angle A/2] = 90^{\circ} + \angle A/2$$

Hence, angle P is always greater than 90°.

Thus, PBC can never be a right angled triangle.

29. Join DE.



$$\angle$$
 BAD = \angle EAC

$$\angle$$
 BAD + \angle DAC = \angle EAC + \angle DAC

$$\angle$$
 BAC = \angle DAE ----- (i)

In ΔABC & Δ ADE

$$AB = AD$$
 (Given)

$$\angle$$
 BAC = \angle DAE (from (i))

$$AC = AE$$

So, By SAS congrience criteria

$$\triangle ABC \cong \triangle ADE$$

$$BC = DE (CPCT)$$



30.

$$m = \frac{1}{2 - \sqrt{3}} \text{ and } n = \frac{1}{2 + \sqrt{3}}$$

$$\therefore 7m^2 + 11mn - 7n^2$$

$$= 7 \times \left(\frac{1}{2 - \sqrt{3}}\right)^2 + 11\left(\frac{1}{2 - \sqrt{3}}\right)\left(\frac{1}{2 + \sqrt{3}}\right) - 7\left(\frac{1}{2 + \sqrt{3}}\right)^2$$

$$= \frac{7}{4 + 3 - 4\sqrt{3}} + \frac{11}{4 - 3} - \frac{7}{4 + 3 + 4\sqrt{3}}$$

$$= \frac{7}{7 - 4\sqrt{3}} + 11 - \frac{7}{7 + 4\sqrt{3}}$$

$$= \frac{7}{7 - 4\sqrt{3}} \times \frac{7 + 4\sqrt{3}}{7 + 4\sqrt{3}} + 11 - \frac{7}{7 + 4\sqrt{3}} \times \frac{7 - 4\sqrt{3}}{7 - 4\sqrt{3}}$$

$$= \frac{7(7 + 4\sqrt{3})}{(7)^2 - (4\sqrt{3})^2} + 11 - \frac{7(7 - 4\sqrt{3})}{(7)^2 - (4\sqrt{3})^2}$$

$$= \frac{7(7 + 4\sqrt{3})}{49 - 48} + 11 - \frac{7(7 - 4\sqrt{3})}{49 - 48}$$

$$= 49 + 28\sqrt{3} + 11 - 49 + 28\sqrt{3}$$

$$= 11 + 56\sqrt{3}$$

